Characterization of the viscoelastic behavior of complex fluids using the piezoelastic axial vibrator

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Synopsis

The piezoelectric axial vibrator (PAV) is a squeeze-flow rheometer working at frequencies \( f \) between 1 and 4000 Hz. It can be used to measure the storage modulus \( G' \) and the loss modulus \( G'' \) of complex fluids in this frequency range. Using polymer solutions with known \( G' \) and \( G'' \) it is shown that the PAV gives reliable mechanical spectra for frequencies between 10 and 3000 Hz. The measurements done with the PAV are combined with a conventional mechanical rheometer \((10^{-3} \leq f \leq 15 \text{ Hz})\) and a set of torsional resonators \((f=13, 25, \text{ and } 77 \text{ kHz})\) to obtain \( G' \) and \( G'' \) between \( 10^{-3} \text{ Hz} \) and \( 77 \text{ kHz} \). Using this combination we present the first analysis of the viscoelasticity of an aqueous suspension of thermosensitive latex particles in this range of frequency. It is demonstrated that the combination of the three devices gives the entire mechanical spectra without resort to the time-temperature superposition principle. © 2005 The Society of Rheology. [DOI: 10.1122/1.1917843]

I. INTRODUCTION

Rheological properties of complex fluids as, e.g., polymer solutions or suspensions of colloid particles give important information about the microstructure and the dynamics of these systems [Ferry (1980)]. They thus provide the base for the applications of these systems. Complex fluids exhibit structural features that range over many orders of magnitude [Larson (1999)]. Their relaxation times span over an equally broad range as well. Measurements of the rheological properties as the storage modulus \( G' \) and the loss modulus \( G'' \) must therefore cover an enormous scale in the time or in the frequency domain in order to capture all relaxation processes in these materials. Considering \( G' \) and \( G'' \) as functions of the frequency \( f \) it is obvious that low values of \( f \) are necessary to attain the first Newtonian region. On the other hand, the modulus \( G' \) measured at high frequencies provides insight into the interparticular forces [Fritz et al. (2003)]. Hence, the high-frequency limiting values \( G'_c \) and \( \eta'_c \) of colloidal suspensions can be used to probe the magnitude of hydrodynamic interactions between the particles and their repulsive potential. Moreover, \( G' \) and \( G'' \) of suspensions of hard spheres measured over a sufficiently
A wide range of frequencies may be evaluated to yield information about the structural arrest of the spheres at high volume fractions [Mason and Weitz (1995a; 1995b)] that can be related to the theory of the glass transition [Goetze and Sjogren (1991)] in these systems.

This brief introduction demonstrates that techniques capable of measuring viscoelasticity of complex fluids over a wide range of frequencies are needed [Fritz et al. (2003); Sohn and Rajagopalan (2004)]. Conventional mechanical rheometers, however, can only access the range of low frequencies (<50 Hz) because of the inertial effects.

Mellema and co-workers have introduced the use of torsional resonators for the study of colloidal suspensions [van der Werff et al. (1989)]. More recent developments in this field have been summarized by Romoscanu et al. (2003). In particular, Willenbacher and co-workers demonstrated that torsional resonators can be used for measurements at high frequencies in the kilohertz range [Fritz et al. (2003)]. The obvious disadvantage of torsional resonators is the fact that these devices can be used only at given frequencies.

Intermediate frequencies have often been accessed by use of the time-temperature superposition principle [Ferry (1980)]. An example for this approach in the field of suspension rheology is the work of Shikata and Pearson (1994) on hard sphere colloids. But in general, the time-temperature superposition principle is not applicable for complex fluids. Therefore measurement techniques that span the entire frequency range without resorting to the time-temperature superposition principle are of central interest in the field of complex fluids.

Microrheological techniques recently introduced by Mason and Weitz (1995a; 1995b); Mason et al. (1996), [Mason (1999)] give access to a wide range of frequencies. Moreover, the mechanical spectra are derived for a continuous range of frequencies. Microrheology, however, relies on the so-called “generalized Stokes–Einstein relation” which may hold only for certain systems. It has been shown to be inadequate for charged colloids [Koenderink et al. (2003)], and its applicability to complex fluids must be checked in each case. Finally, for the intermediate frequency only a few instruments were able to give a continuous and reliable measurement as, e.g., the piezorheometer described in the work of Cagnon and Durand (1980) or the piezoelectric rotary vibrator [Kirschenmann (2002)] both working in shear strain.

Recently, Pechhold and co-workers introduced a new device named “piezoelectric axial vibrator” (PAV). It consists of a dynamic press with a thin gap in which the liquid is confined. A squeeze flow is generated by a piezoelectric drive and the answer of the system measured by piezosensors can be evaluated to lead to $G'$ and $G''$ between 10 and 4000 Hz. In this way the PAV closes the gap in the frequency range of conventional rheometers and the torsional resonators. In principle, the concept of the PAV is very appealing and the frequency range accessible by this instrument is exactly in the range that must be probed for the study of typical complex fluids. Based on earlier work by Kirschenmann (2003) we present a comprehensive test of the PAV as applied to typical complex fluids as polymer solutions and colloidal suspensions. We compare the results obtained with this instrument to data from conventional rotational rheometry at low frequencies and from a set of torsional resonators at high frequencies. Moreover, the data obtained from rotational rheometry at various temperatures are shifted according to the time temperature superposition principle in order to cover the same frequency range as the PAV.

The purpose of this paper is twofold: (i) At first we examine the reliability of the PAV and its possible limitations and (ii) we demonstrate that the combination of the three rheometers, namely the mechanical spectrometer, the PAV, and the torsional resonators provide a convenient and reliable access to the viscoelastic properties of complex fluids.
over 5–7 orders of magnitude in frequency. This will be further demonstrated by analyzing the viscoelasticity of a suspension of thermosensitive particles.

II. THEORY

The general theory of squeeze flow is well exposed in standard textbooks of rheology [Bird et al. (1987)] and the theory of the PAV has been already presented in the work of Kirschenmann (2003). Here it suffices to delineate the main features.

Figure 1 gives a scheme of the PAV. The lower plate oscillates with constant force amplitude $F\hat{=}$. When the PAV is unloaded, the dynamic displacement $x\hat{=}0$ of the lower plate is measured at a given frequency leading to the compliance $x\hat{=}0/F\hat{=}$. The same measurement is repeated at the same frequencies with the material under consideration filling the gap (see Fig. 1). This gives the modulated compliance $\dot{x}/F\hat{=}$. From the complex ratio $x\hat{=}0/x\hat{=}0$, the complex squeeze stiffness $K^*$ of the material can be calculated by use of an appropriate mechanical equivalent circuit (see Fig. 1) and solving its equations of motion (1) [Kirschenmann (2003)]:

$$\begin{cases} -\omega^2m_1x_1 = -K^*(x_1 - x_0) - K_1x_1 \\
-\omega^2m_0x_0 = -K^*(x_0 - x_1) - K_{01}(x_0 - x_2) + F \\
0 = -K_{01}(x_2 - x_0) - K_{02}x_2 - F. \end{cases}$$ (1)

For linear viscoelasticity this calculation leads to the formula

$$K^* = \frac{3\pi}{2}R\left( \frac{R}{d} \right)^3 G^*/\left( 1 + \frac{\rho\omega^2d^2}{10G^*} + \ldots \right),$$ (2)

where $R$ is the radius of the plate, $d \ll R$ is the gap width, $\rho$ is the density of the squeezed material, and $G^*$ is its complex shear modulus. The expression of the numerator agrees with that derived in the literature [Bird et al. (1987)], [Laun et al. (1999)]. The denominator contains the first term (slit approximation) of a series expansion that takes into account the inertia of the material in the gap. This effect may become important at very high frequencies.

Equation (2) tacitly assumes an incompressible material and hence only considers the complex shear modulus $G^*$ or the complex compliance $J^* = 1/G^*$. For precise measure-
ments, however, the dynamic compressibility $\kappa^*$ must be introduced as well. For squeeze flow (in the limit of small amplitudes) one obtains [Kirschenmann (2003)]:

$$\frac{1}{K^*} = \frac{2}{3\pi R^4} \left( \frac{1}{G^*} + \frac{3}{2} \frac{R^2}{d^2} \kappa^* \right).$$

(3)

Equation (3) demonstrates that the correction due to a finite compressibility depends strongly on the ratio $R/d$. Its magnitude can be obtained through performing measurements at different gap thickness $d$.

III. EXPERIMENT

A. Instruments

The PAV is a dynamic press working at frequencies between 1 and 4000 Hz. The actor/sensor is a thin-walled quadratic copper tube carrying on top a thick stainless steel plate, which serves as the lower boundary of the sample gap (see Fig. 2). As shown in
Fig. 2(b), four piezoelements are attached to two opposite walls of the tube in order to exert the vibrations while four additional piezos are fixed to the remaining sides in order to pickup the response signal. Direct coupling of excitation and detection is avoided by four lengthwise cuts of the tube [see Fig. 2(b)].

This lower part of the device is surrounded by a double walled cylinder allowing the circulation of a thermostating fluid. The whole setup is covered by a thick metal lid, which is the upper boundary of the gap and provides a complete sealing of the fluid. The rigidity $K_0$ of the cylinder must at least attain $1.10^8 \text{ N m}^{-1}$ to assure a high resonance frequency for the head of the probe and the sensor cylinder. Therefore the sample rigidity, $K^*$, should be lower than $10^9 \text{ N m}^{-1}$.

The PAV is operated by a lock-in-amplifier. The exciting voltage of the driving piezos is proportional to the axial force. The measured voltage of the piezos that monitor the deformation is the signal used for determining $K^*$. The width $d$ of the gap of the squeeze-flow rheometer is defined by the lid mounted onto the rheometer (see Fig. 2). In order to vary the gap, several rings of 10, 35, 50, 100 $\mu$m thickness can be used. The variation of the gap turned out to be necessary in order to perform the measurements in the correct range. Systems with low viscosities must be measured using a small $d$ whereas higher viscosities needed a wider gap (see later). Hence, variation of the gap width between 20 and 200 $\mu$m covers measurements of the viscosity in the range between 1 and 2000 mPa s. The required sample volume is on the order of 100 $\mu$L depending on the width of the gap. In all case the amount of liquid was accurately adjusted by a microsyringe. The temperature was controlled with an accuracy of $\pm 0.02 ^\circ \text{C}$.

B. Calibration of the instrument and accuracy

The instrument was calibrated using Newtonian liquids of different viscosity to determine the optimal gap for each range of viscosities. For this purpose a set of different glycerol/water mixtures was used. The viscosities of these mixtures are summarized in Table I.

<table>
<thead>
<tr>
<th>Weight fraction of glycerol</th>
<th>$\eta$ at 20 $^\circ \text{C}$ (mPa s)</th>
</tr>
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<tbody>
<tr>
<td>0</td>
<td>1.005</td>
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<tr>
<td>35</td>
<td>3.040</td>
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<tr>
<td>50</td>
<td>6.050</td>
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<td>75</td>
<td>36.46</td>
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<td>85</td>
<td>112.9</td>
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<td>95</td>
<td>545</td>
</tr>
<tr>
<td>100</td>
<td>1499</td>
</tr>
</tbody>
</table>

In order to compare the viscosities obtained by the PAV to data from other systems, two rheometers have been employed: A rheometrics fluid spectrometer for the range of low frequencies (0.01–15 Hz), and the torsional resonators introduced recently by Willenbacher and co-workers [Fritz et al. (2003)] for the region of high frequencies. In the following we give a brief description of the measurements using these devices.

The Fluids Spectrometer RFS II from Rheometrics Scientific is a strain-controlled rotational rheometer equipped with a Couette system (cup diameter: 34 mm, bob diameter: 32 mm, bob length: 33 mm). Strains are applied in the range starting from 500% for
the low viscosity liquids to provide an accurate response up to 0.5% for the more viscoelastic solutions. For each measurement the deformation was set to remain in the linear viscoelastic regime. Measurement were performed on 10 mL of the fluid and the temperature was set with an accuracy of ±0.05 °C.

Two torsional resonators supplied by the Institut für dynamische Materialprüfung, Ulm, Germany, have been used to obtain data at high frequencies \( f \) [Fritz et al. (2003)]. Two geometries are available (cylinder or double-dumbbell) allowing for measurements at 13, 25, and 77 kHz. The penetration depth of the shear wave is typically on the order of 50 \( \mu \text{m} \) for the samples investigated here. This ensures that the method probes the viscoelastic properties of the bulk phase. The measuring cell, however, is much larger than this penetration depth and no disturbance may result from the walls of the container. The small amplitudes of the torsion of the cylinder (≈50 nm) ensure that the maximum strain is small. The measurements are hence taken in the linear viscoelastic regime. The experimental procedure and the evaluation of data have been described recently [Fritz et al. (2003)].

The real part of the complex viscosity of water-glycerine mixtures is plotted against the frequency in Fig. 3. Here data obtained by all the three devices are presented. The gaps of the PAV was varied \( (d=20, 35, 50, 100, \text{ and } 200 \mu\text{m}) \) in order to adjust for the viscosity of the sample ranging from 1 to 1500 mPa s (dashed lines in Fig. 3). The viscosity was calculated using Eq. (2) and the width \( d \) of the gap was slightly adjusted so that the experimental value was matched. This calibration of the width of the gap is used in subsequent measurements. Moreover, results obtained for one sample but different gap widths demonstrated that the contribution due to the dynamic compressibility [cf. Eq. (3)] is negligible for these Newtonian liquids as expected.

Figure 3 also delineates the optimal domains of the measurement of the PAV by dashed lines. In these domains the measured viscosity is independent of the frequency. In
the following only data from these optimal domains will be shown. The good correspondence between the three apparatus illustrates the quality of the measurements provided by the PAV for the Newtonian solutions.

C. Viscoelastic fluids: Polystyrene solution

We use a commercial polystyrene grade (PS 148 H from BASF) dissolved in ethylbenzene as a benchmark system to check the accuracy of the measurements of $G'$ and $G''$ by the PAV. Concentrated polymer solutions present well-studied examples of viscoelastic fluids that exhibit moduli varying over many orders of magnitude with increasing frequency [Graessley (1974)].

The ethylbenzene used was of commercial grade without special purification. The solution contains 30% polystyrene with $M_w = 148,000$ g/mol. Solutions of polystyrene were carefully studied and precise data based on the time-temperature superposition principle are available [Graessley (1974); Baumgärtel and Willenbacher (1996)].

$G'$ and $G''$ of this solution as the function of frequency was obtained as follows: Rheological measurements with a mechanical rheometer were done at $-80$, $-50$, and $24$ °C. In order to obtain a wide range of frequencies, the frequency-temperature superposition principle has been used as already discussed by Baumgärtel and Willenbacher (1996). The temperature dependence can be described by a universal, concentration invariant Williams–Landel–Ferry-shift parameter $a_T$ [Williams et al. (1955)]:

$$\log_{10} a_T = \frac{-c_1(T - T_{\text{ref}})}{c_2 + T - T_{\text{ref}}}.$$  \hspace{1cm} (4)

We have chosen $T_{\text{ref}} = 20$ °C and obtain $c_1 = 1.47$ and $c_2 = 143$ K.

Figure 4 displays $G'$ and $G''$ as the function of the frequency. Data at low frequency have been obtained by the mechanical spectrometer RFS II whereas the three points referring to the highest frequencies have been measured using the torsional resonators. The data at intermediate frequencies have been obtained with the PAV using the optimal
The width of the gap (see the discussion of Fig. 3). The data obtained by the three widely different instruments fit together within the limits of error of the respective devices. The lines give the respective values of $G'$ (dashed) and $G''$ (full) derived from Eq. (4). Good agreement is seen over six orders of magnitude. There are only small deviations between the measured data and the spectra calculated from the time-temperature superposition principle. We assign these small discrepancies to the limitation of Eq. (4) and to the experimental uncertainties in obtaining the moduli in such a wide temperature range.

Figure 5 demonstrates that the width $d$ of the gap has a minor influence on the resulting values of $G'$ and $G''$. Here $G'$ and $G''$ obtained from the poly(styrene) solution by the PAV for different width of the gap are plotted against the frequency $f$. Evidently, $G'$ and $G''$ do not depend on $d$ within the given limits of error. The maximum of error amounts to 20% if the width of the gap is not optimal. This further confirms the reliability of the instrument and justifies the neglect of the dynamic compressibility [cf. Eq. (3)].

Thus, the earlier discussion has established two criteria for the accuracy of the measurement: First, the optimal width of the gap is obtained by measurement of Newtonian
liquids. The small corrections for the width of the gap, which followed from this calibration demonstrates that Eq. (2) provides a accurate description of the flow in the instrument. Second, the measured spectra of $G'$ and $G''$ must be independent of the width $d$. This is seen indeed in Fig. 5 and the residual discrepancies at low frequency can be traced back to a width of the gap which is not optimal.

From these data and the foregoing comparison using a polystyrene solution as a benchmark system we conclude that the PAV gives reliable data for polymer systems that exhibit a marked viscoelastic behavior. The range of concentrations that can be studied is only limited by the smallest gap available (see the discussion of Fig. 3). Hence, highly dilute polymer solutions in which the viscosity exceeds hardly the one of the solvent cannot be measured with the PAV with sufficient accuracy [see the discussion of this problem in Stokich et al. (1994)].

D. Methylcellulose in solution

Aqueous solutions of methylcellulose (MC) gel upon heating [Leibler et al. (1991)]. The gelation is thermoreversible and ascribed to the presence of hydrophobic interactions. The rheology of this system was already investigated in a study of Desbrières [Desbrières et al. (1999)] and the rheological experiments were carried out on the piezorheometer built by Palerme [Bartolino and Durand (1977); Cagnon and Durand (1980; 1981)]. Hence, these solutions provide another benchmark system.

Methylcellulose has been purchased from Sigma-Aldrich. The weight average molecular weight of MC is 86 000 g mol$^{-1}$. The degree of substitution is ranging from 1.6 to 1.9 as indicated by the manufacturer. It was purified by dialysis in order to remove salts and other low molecular weight impurities. Solutions of $\sim$2 wt % of methylcellulose were prepared in de-ionized water and stirred for 2 days to ensure a homogeneous solution. This solution was then packed in Spectra/Por® dialysis tube membranes which were bought from Spectrumlabs (MWCO-2000). Dialysis was carried out until the conductivity of water became equal to pure de-ionized water. Later the solution was dried in a vacuum oven at 80 °C. The pure methylcellulose was then stored for further use. The measurements were performed on a solution of 1.5 wt % at 20 °C. Again the range of frequencies was covered by measurement using the three instruments.

The rheogram shown in Fig. 6 is typical of an entangled polymer solutions. As can be seen from Fig. 6, a good correspondence between the three instruments is seen. The residual differences between the instruments are within their respective limits of error. This demonstrates again that concentrated polymer solutions can be measured by the combination of the three instruments.

Following earlier work [Desbrières et al. (1999)] a general Maxwell’s model was used to describe the data. The expression that includes the high-frequency contribution reads

$$\eta^* = \frac{\eta_0}{1 + (i \omega \tau_0)^{-h}} + \eta_v,$$

(5)

where $\eta_0$ is the zero-shear viscosity and $\eta_v$ denotes the high-shear viscosity. Finally, $\tau_0$ is the average time of relaxation and the parameter $h$ describes the width of the relaxation time distribution. Figure 6 demonstrates that Eq. (5) provides a good description of the results over the entire range of frequencies under consideration here. This is in agreement with the earlier studies [Desbrières et al. (1999)].
E. Thermosensitive latex particles

As an example for a complex fluids we analyze here a thermosensitive latex that has been under scrutiny recently [Senff et al. (1999)]. The particles consist of a solid poly(styrene) core and a shell composed of crosslinked poly(N-isopropylacrylamide) (PNIPA) chains. Suspended in water these particles swell when lowering the temperature below room temperature through the uptake of water in the shell. Going to temperatures above 25–30 °C leads to a marked decrease of the particles radius because the water is expelled from the thermosensitive PNIPA-layer again. This swelling transition within the layer is fully reversible [Dingenouts et al. (1998); Seelenmeyer et al. (2001)] and can be used to adjust the effective volume fraction \( \phi_{\text{eff}} \) of the particles by increasing or lowering the temperature [Senff et al. (1999)]. Evidently, the time-temperature superposition principle cannot be applied for determining \( G' \) and \( G'' \).

The core-shell latex used in this study was prepared as described recently [Dingenouts et al. (1998); Seelenmeyer et al. (2001)]. The core particles has a radius of 52.5 nm and the shell a thickness of 52.8 nm at 10 °C as determined by light scattering. The degree of crosslinking was 2.5 mol % with regard to monomer N-isopropylacrylamide. The latex was purified by ultrafiltration. The weight concentration of the latex was 10.9 wt %. The corresponding effective volume fraction \( \phi_{\text{eff}}=(4 \pi/3)R_H^3 \) could be determined from the hydrodynamic radius \( R_H \) available from dynamic light scattering [Seelenmeyer et al. (2001)]. For the suspension under consideration here \( \phi_{\text{eff}}=0.585 \) at a temperature of 10 °C.

The rheological measurements were realized with the set of the three instruments. A period of 1 h was allowed for thermal equilibrium before starting each measurement. Figure 7 displays \( G'(\omega) \) and \( G''(\omega) \) obtained in this way over the entire range of frequencies. As already discussed by Mason and Weitz (1995a; 1995b), a suspension of hard spheres in the vicinity of the glass transition should exhibit the features seen in Fig. 7: The storage modulus \( G' \) is expected to exhibit a marked plateau for a rather wide range of frequencies while \( G'' \) is expected to go through a pronounced minimum.
The model proposed by Mason and Weitz (1995a; 1995b) can be used for the quantitative description of the data thus obtained. It is based on the combination of three major effects. The low frequency behavior is described within mode coupling theory (Goetze 1999). It assumes that the stress autocorrelation function has the same functional form as the density autocorrelation function. The high-frequency data analysis is complicated due to an anomalous contribution to both $G'$ and $G''$ proportional to $\omega^{0.5}$ which arise from a diffusional boundary layer between the spheres (Lionberger and Russel 1994). The high frequency suspension viscosity $\eta_s$ leads to a contribution to $G''$ that is proportional to $\omega$. It can be taken from the experimental data obtained at highest frequencies by use of the torsional resonators. The resulting expressions for $G'$ and $G''$ are (Mason and Weitz 1995a; 1995b):

$$G'(\omega) = G_P + G_\sigma \left[ \Gamma(1-a')\cos\left(\frac{\pi a'}{2}\right)(\omega t_\sigma)^{a'} - B\Gamma(1+b')\cos\left(\frac{\pi b'}{2}\right)(\omega t_\sigma)^{-b'} \right] + G_D'(\omega)$$

and

$$G''(\omega) = G_\sigma \left[ \Gamma(1-a')\sin\left(\frac{\pi a'}{2}\right)(\omega t_\sigma)^{a'} + B\Gamma(1+b')\sin\left(\frac{\pi b'}{2}\right)(\omega t_\sigma)^{-b'} \right] + G_D''(\omega) + \eta_s\omega,$$

where $\Gamma(\alpha)$ is the gamma function, $a' = 0.301$, $B = 0.963$, as and $b' = 0.545$ are parameters predicted for suspensions of hard spheres (Goetze and Sjoegren 1991). $G_\sigma$ is a fit parameter. The storage modulus has an inflection point at the plateau value $G_P$, and the frequency at the minimum of the loss modulus is set by the value of the plateau, $1/t_\sigma$. Following Mason and Weitz (1995a; 1995b) the frequency dependence of $G_D'$ and $G_D''$ for hard sphere suspensions is used here as given by Lionberger and Russel (1994) and by De Schepper et al. (1993):
where $\tau_D=a^2/D_S$, is the diffusional time determined by the $\phi$-dependent short-time diffusion coefficient with $a$ being to the radius of the particles. The radial pair distribution function at contact is approximated by $g(2a, \phi) = 0.78/(0.64- \phi)$ again mapping this suspension onto an effective hard sphere system [see the discussion of this point by Mason (1999)]. Moreover, we equate $\phi = \phi_{\text{eff}}$. Hence, $G_\sigma$ and $D_s$ are the only free fit parameter remaining here.

Figure 7 demonstrates that there is good agreement between the data obtained by the three instruments. Moreover, good agreement is seen over eight orders of magnitude. The lines give the respective values of $G'$ (solid line) and $G''$ (dashed line) derived from Eqs. (6) and (7). This agreement is more remarkable when considering that only two fit parameters had to be used in this comparison. Hence, the model of Mason and Weitz (1995a; 1995b) based on the mode-coupling theory explains the measured viscoelasticity of suspensions very well.

IV. CONCLUSION

A new rheometer, the PAV, has been introduced and tested by using Newtonian liquids and viscoelastic polymer solutions. The data presented here demonstrate that the PAV works reliably between 10 and 3000 Hz. It thus closes the gap between conventional mechanical spectrometers and the torsional resonators. The combination of all three devices gives access to $G'$ and $G''$ as the function of frequency over 7–8 orders of magnitude. This provides a sound basis for a comprehensive study of the viscoelasticity of complex fluids as was shown for the case of polymer solutions and suspensions of colloidal particles.

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